



SEAN NAV
BENCH

Socially Acceptable Bipedal Navigation: A Signal-Temporal-Logic-Driven Approach for Safe Locomotion

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 - Imitate human path



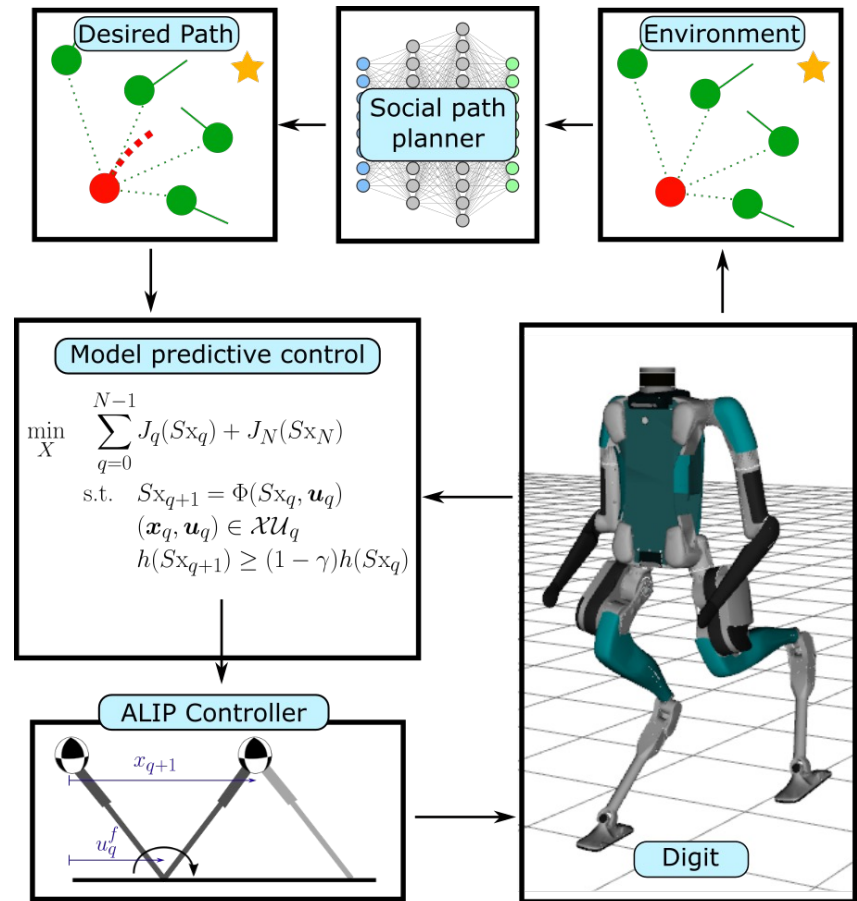
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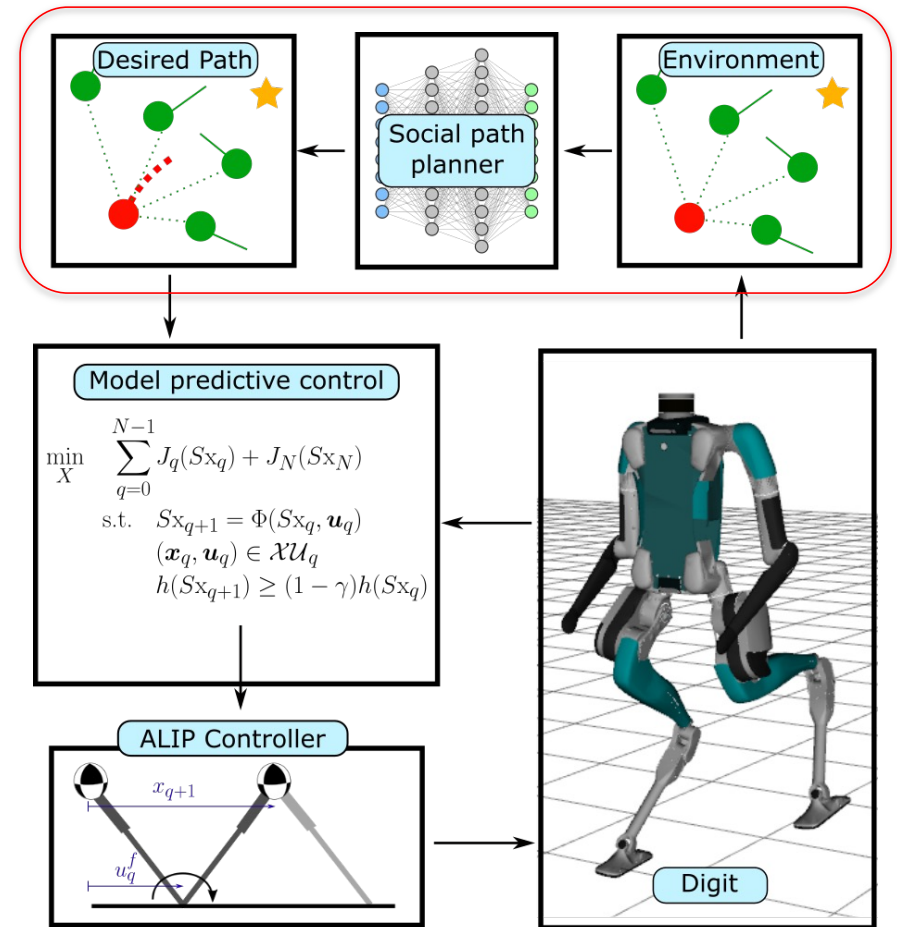


Hierarchical Planning



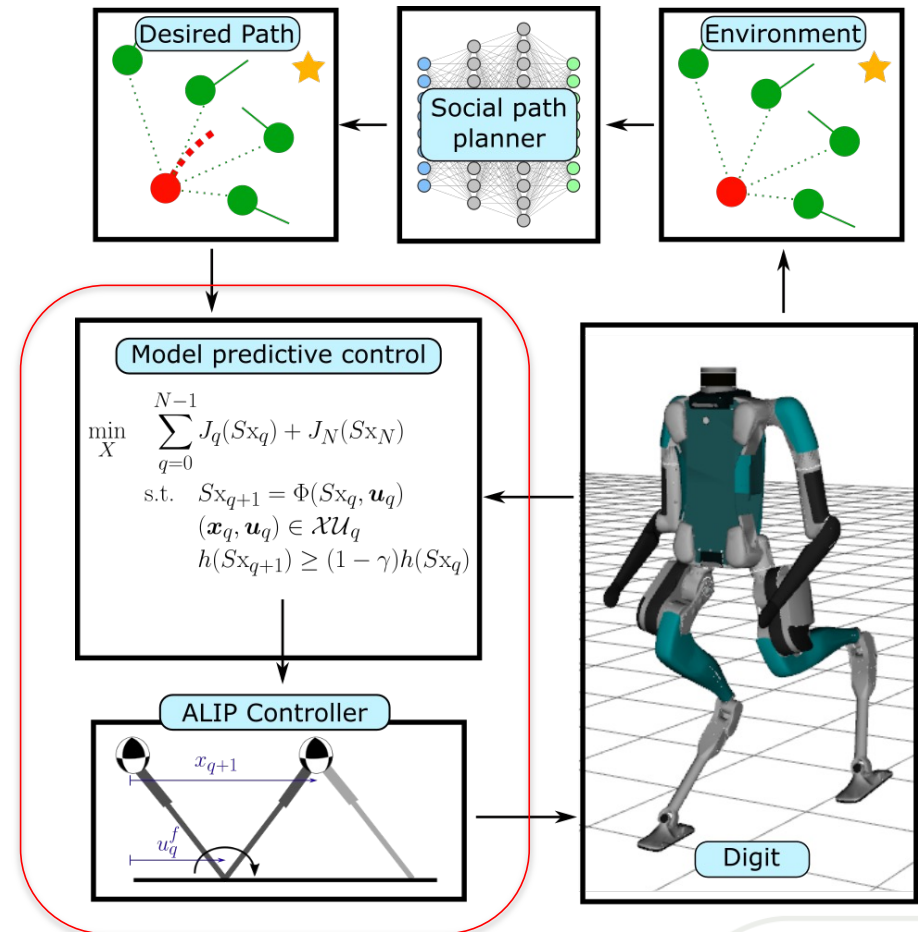
Hierarchical Planning

- High level: learning-based-social-path planner
 - Generates a **socially acceptable** path and **promotes** locomotion safety



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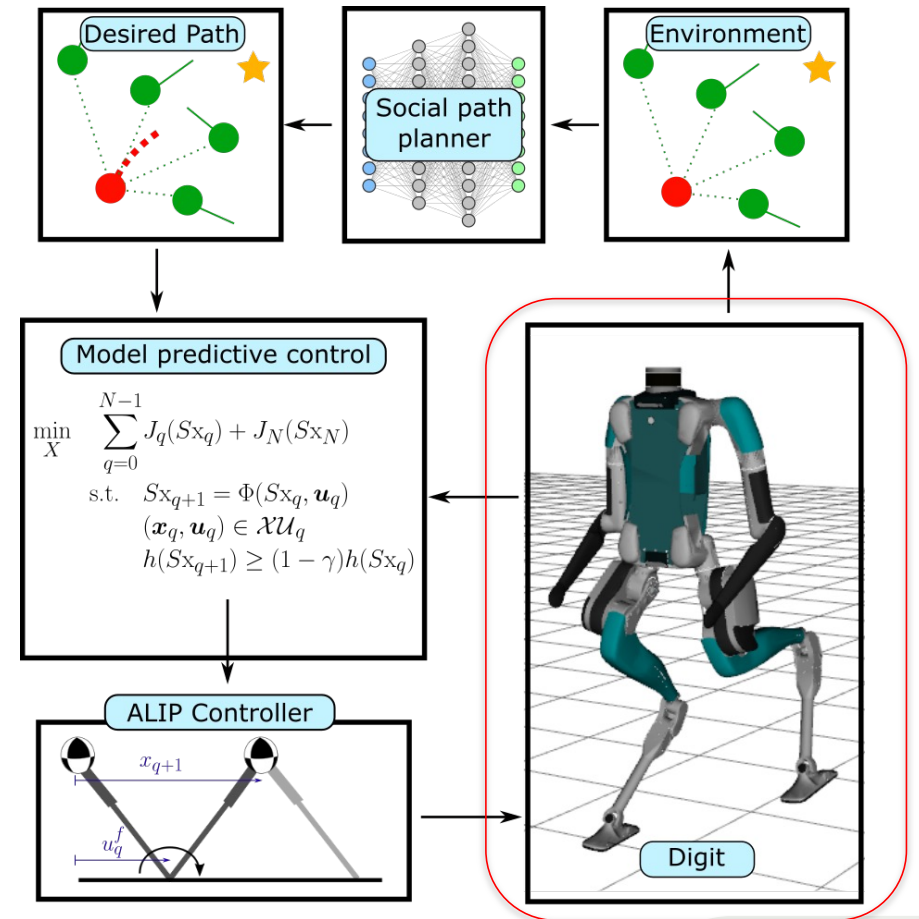
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 - **Guarantees** task completion, and navigation and locomotion safety for the reduced order model



[1] Narkhede, Kunal S., et al. RAL 2022
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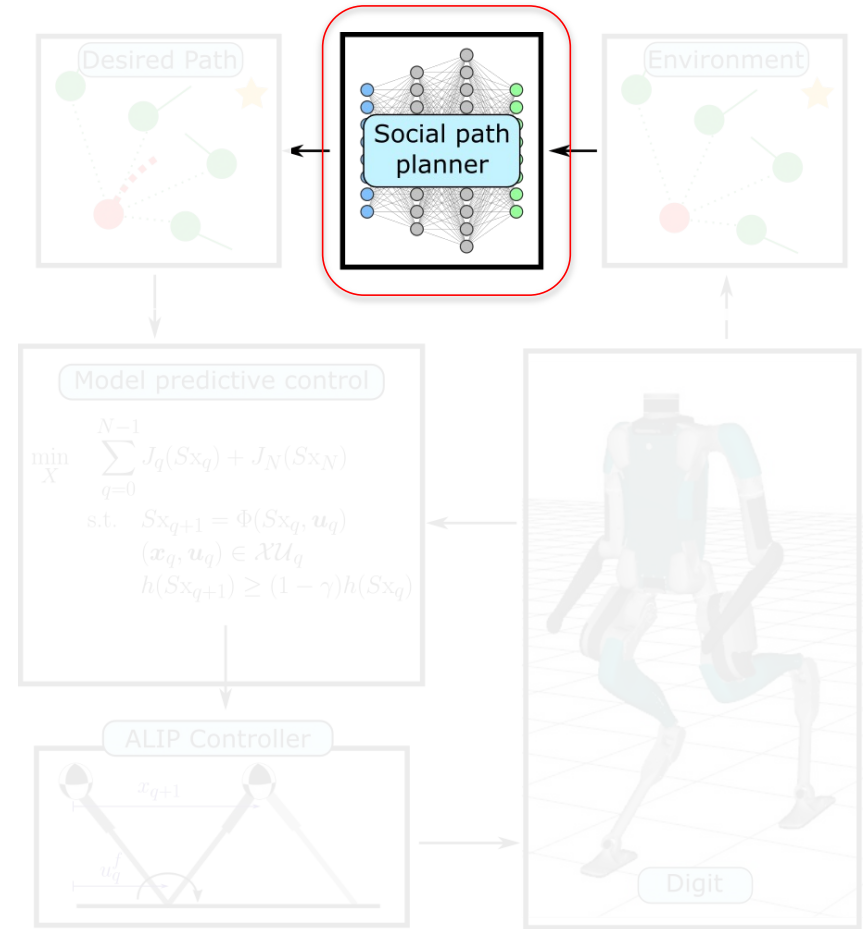
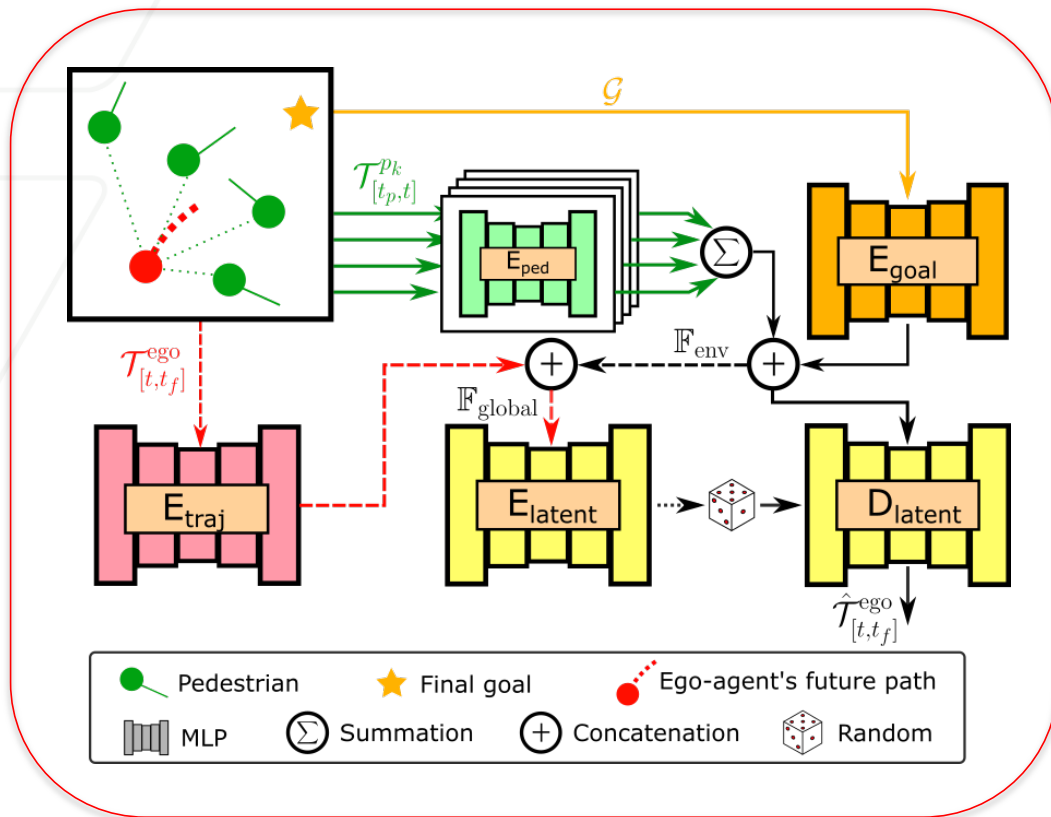
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- Low level: passivity-based realtime controller [2, 3]
 - **Tracks** the reduced-order-model trajectory from the middle level

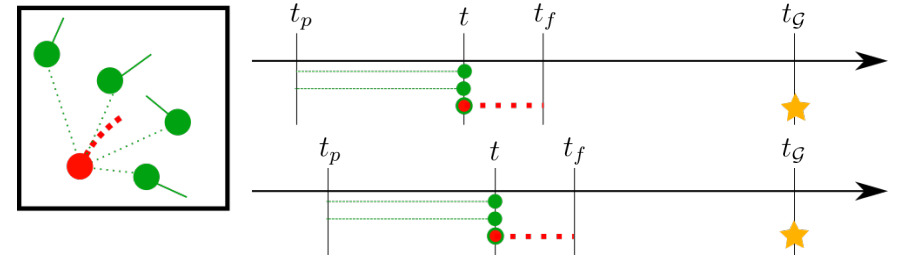


[1] Narkhede, Kunal S., et al. RAL 2022
 [2] Y. Gong and J. W. Grizzle, JDSMC 2022
 [3] A. Shamsah., et al. TRO 2023

Social Path Planner



Social Path Planner



pedestrians' past path

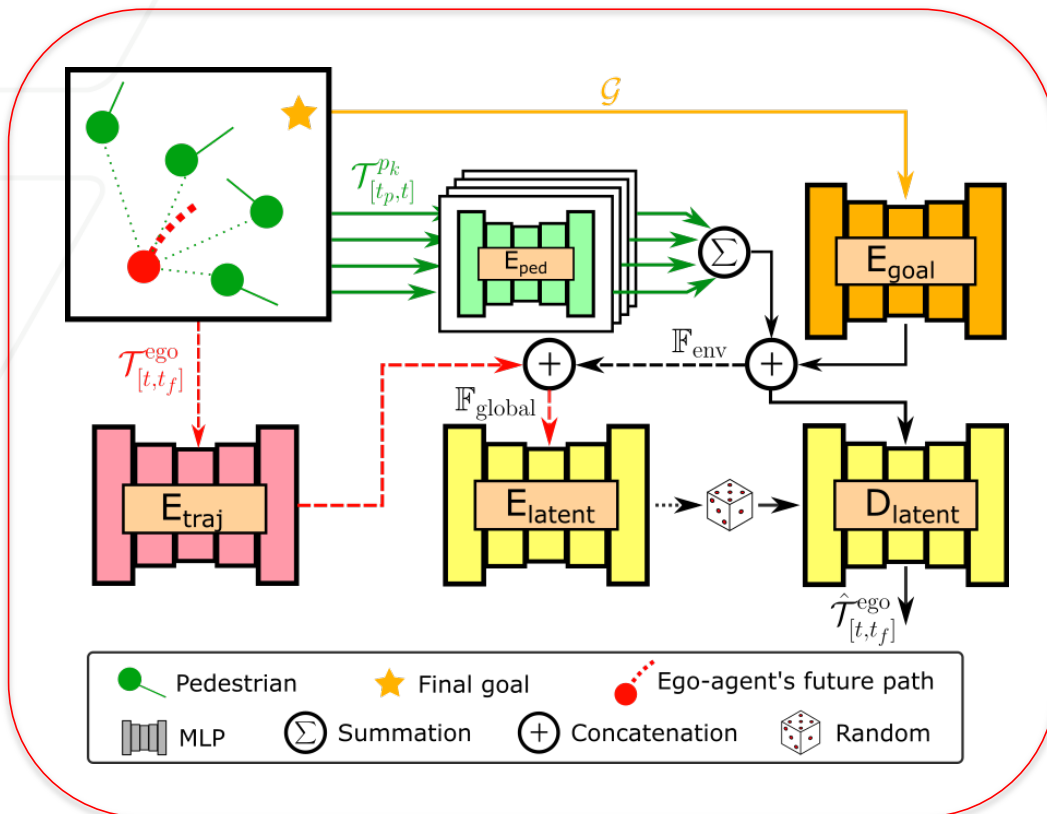
$$(x_{[t_p, t]}^{pk}, y_{[t_p, t]}^{pk}) = \mathcal{T}_{[t_p, t]}^{pk}$$

ego-agent's final destination

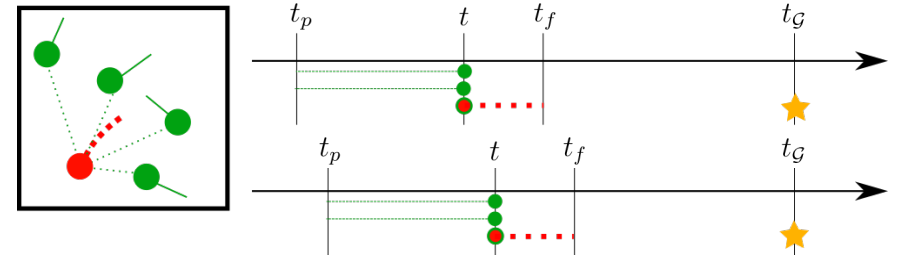
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ego-agent's future path

$$(x_{[t, t_f]}^{\text{ego}}, y_{[t, t_f]}^{\text{ego}}) = \mathcal{T}_{[t, t_f]}^{\text{ego}}$$



Social Path Planner



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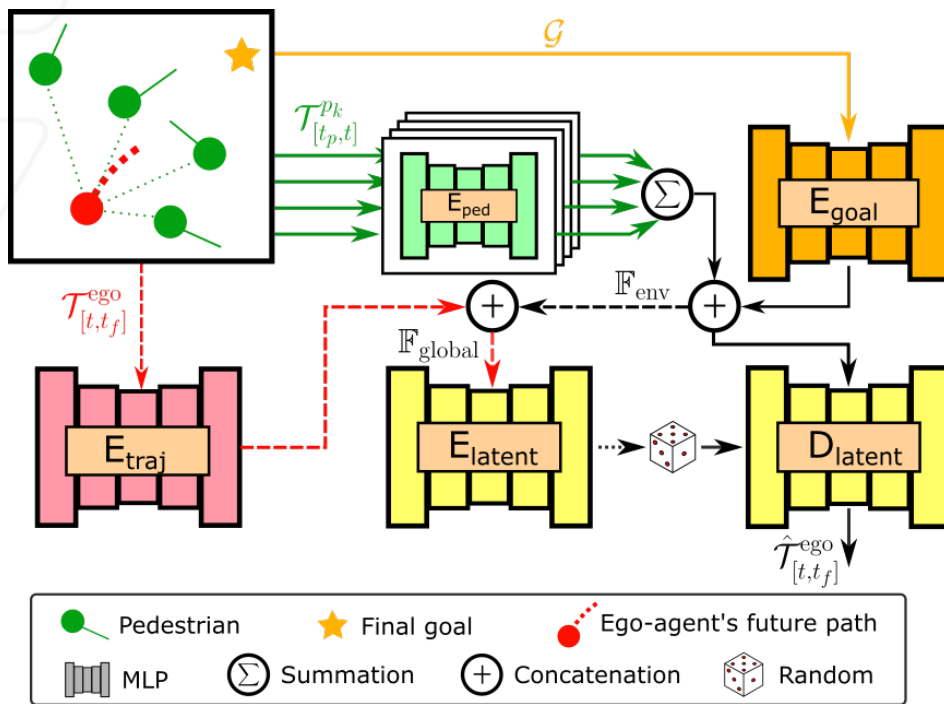
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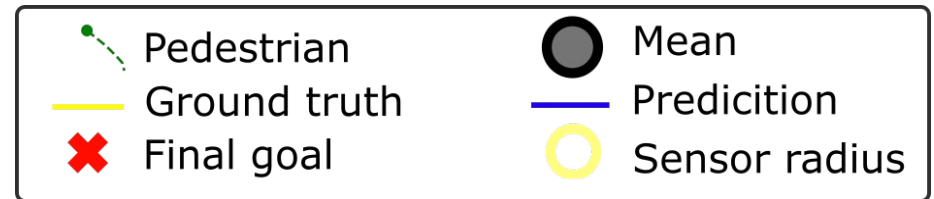
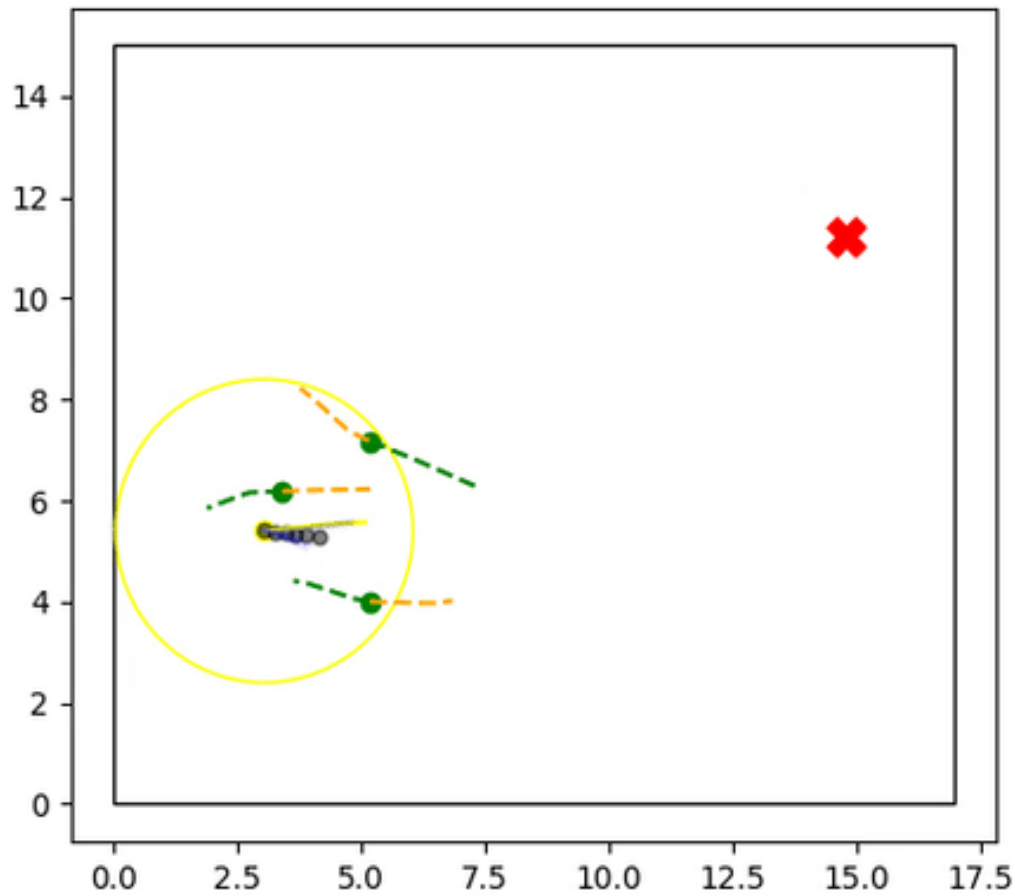
ego-agent's future path

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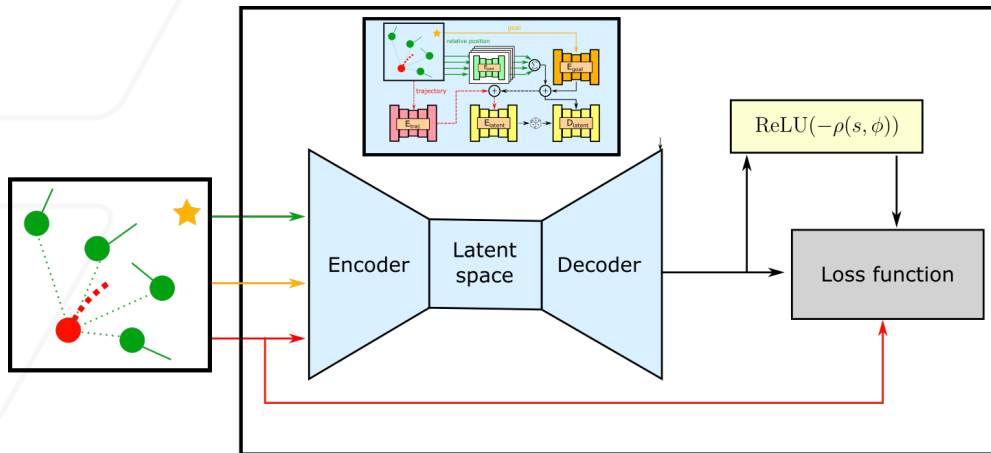
Assumption: A socially-acceptable path for the ego-agent is the path that a human would take in a similar setting



Social Path Planner Results

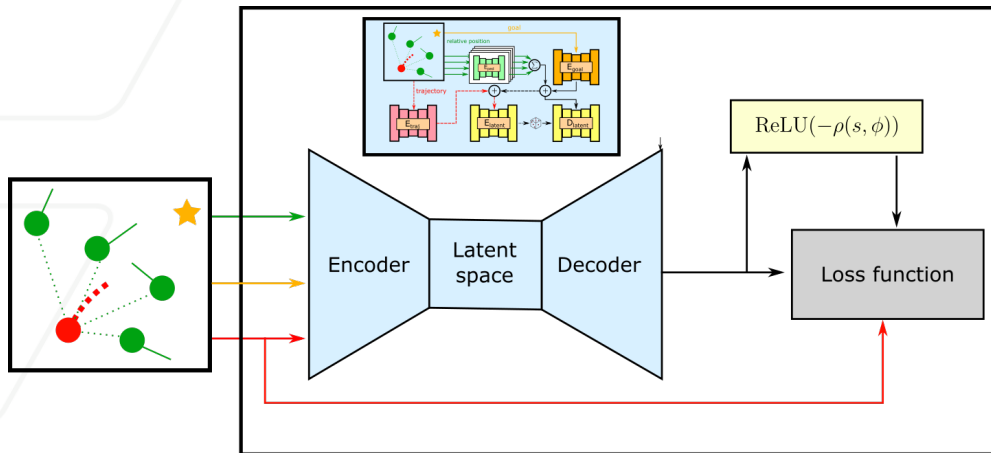


Incorporating Locomotion Safety Specifications



- **Motivation:** regulate the CVAE output to promote **locomotion safety**
- **Methodology:** use the quantitative semantics of Signal-Temporal Logic (STL) as **part of the loss function** [4]

Incorporating Locomotion Safety Specifications

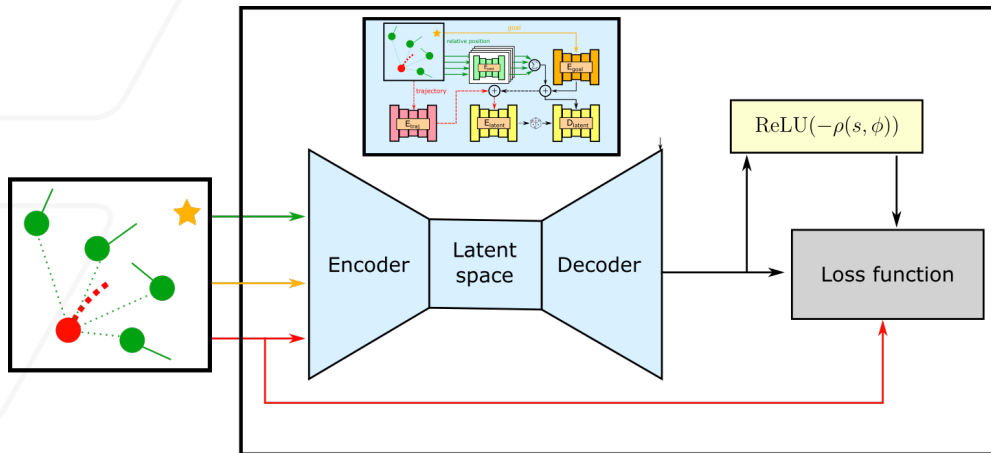


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$\rho(s_t, \phi)$ quantifies **the degree of satisfaction or violation** of the specification ϕ given a specific signal s_t

$$\rho(s_t, \phi) = \begin{cases} \geq 0 & s_t \text{ satisfies } \phi \\ < 0 & s_t \text{ violates } \phi \end{cases}$$

Incorporating Locomotion Safety Specifications



- Locomotion velocity specifications

$$\phi_{\text{sag}} = \square_{[t+1, t_f]} (s_{[t+1, t_f]}^{v_{\text{sag}}} \leq v_{\text{max}} \wedge s_{[t+1, t_f]}^{v_{\text{sag}}} \geq v_{\text{min}})$$

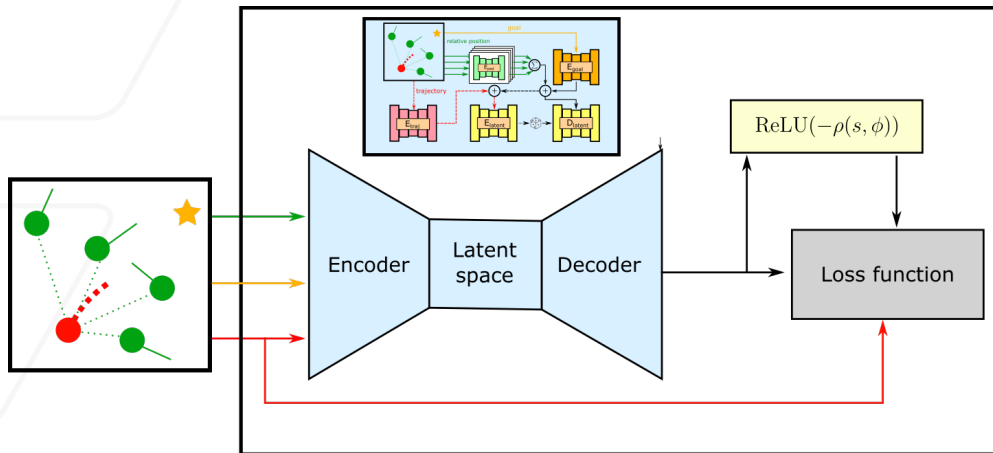
$$\phi_{\text{lat}} = \square_{[t+1, t_f]} (s_{[t+1, t_f]}^{v_{\text{lat}}} \leq v_{\text{lat}} \wedge s_{[t+1, t_f]}^{v_{\text{lat}}} \geq -v_{\text{lat}})$$

$$\phi_{\text{vel}} = \phi_{\text{sag}} \wedge \phi_{\text{lat}}$$

- Heading change specifications

$$\phi_{\Delta\theta} = \square_{[t+1, t_f]} (s_{[t+1, t_f]}^{\Delta\theta} < \Delta\theta_{\text{max}} \wedge s_{[t+1, t_f]}^{\Delta\theta} > -\Delta\theta_{\text{max}})$$

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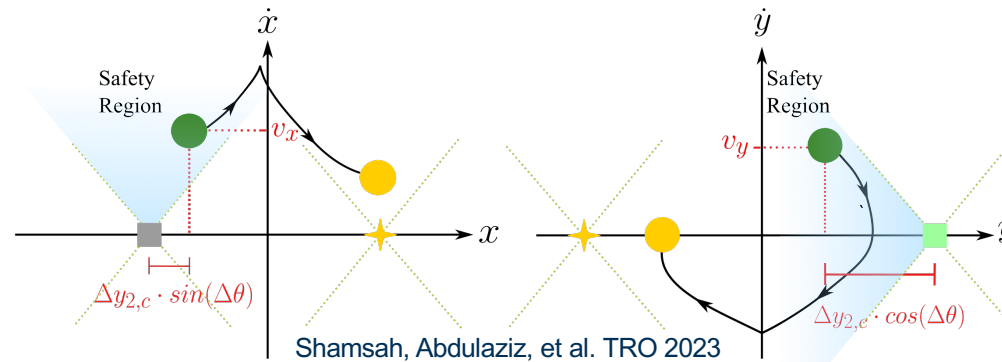
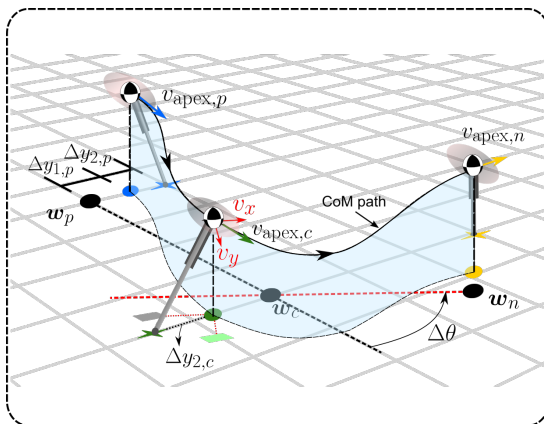
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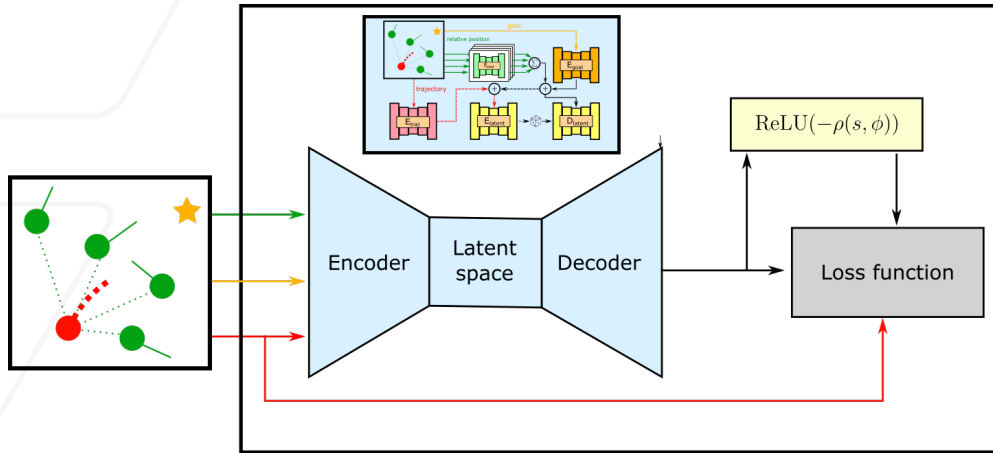
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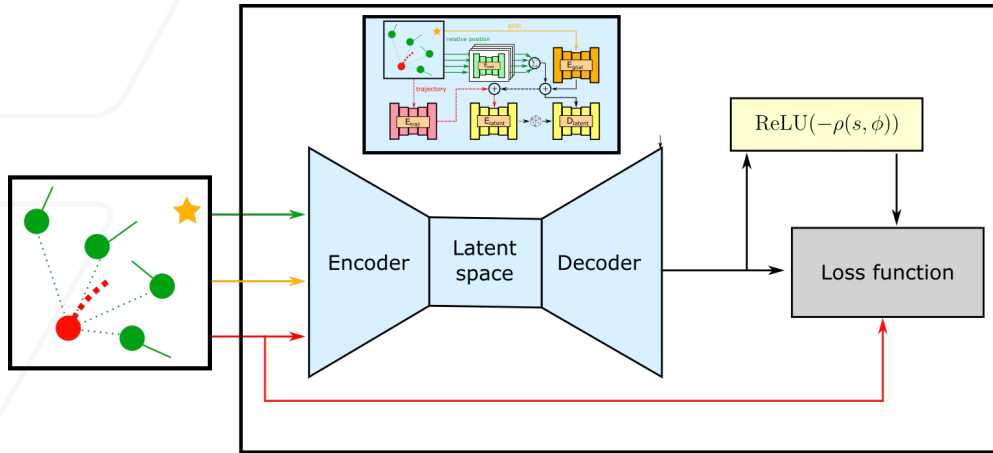
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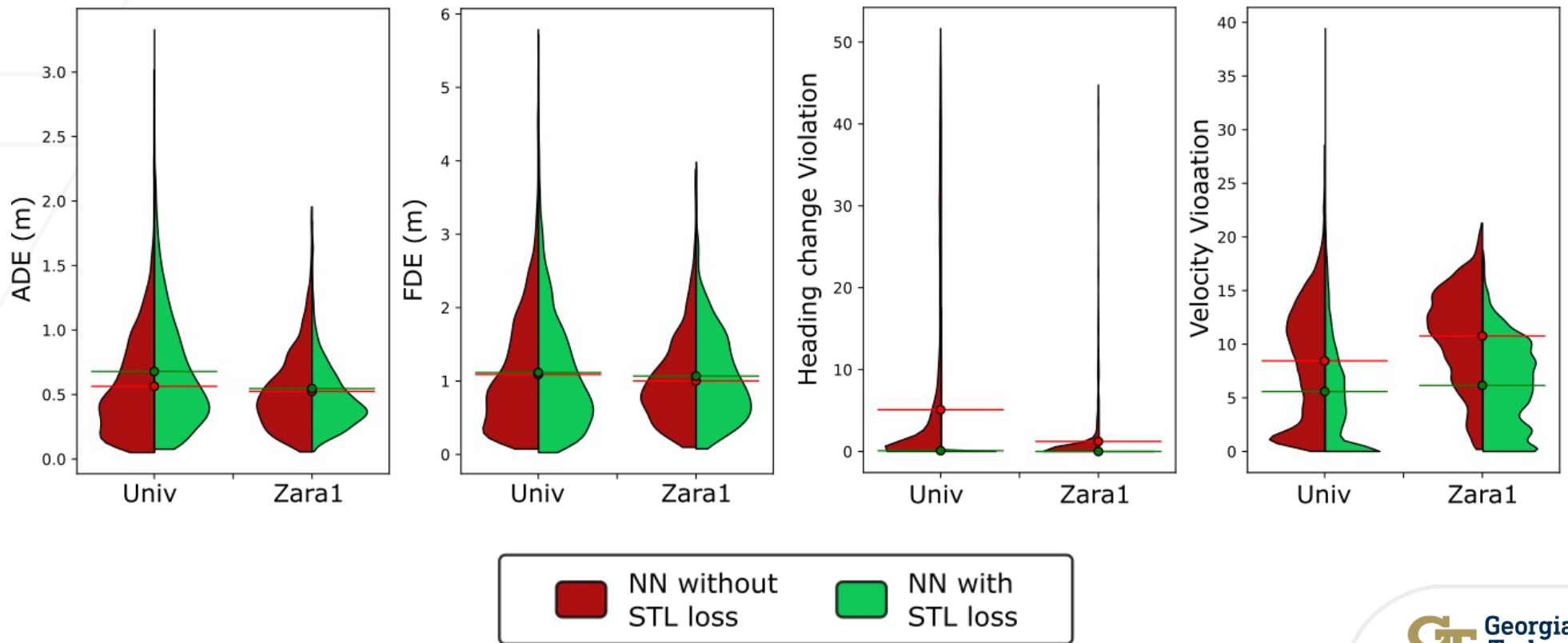
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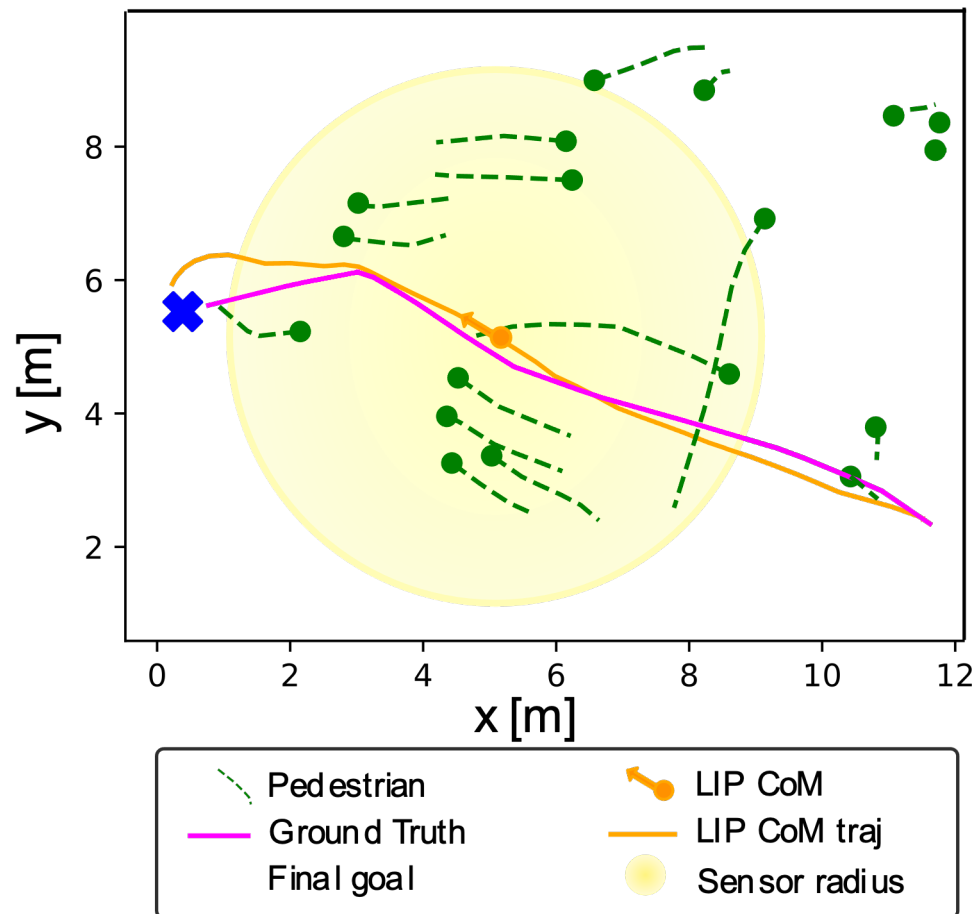
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$$\mathcal{L}_{\text{STL}} = \alpha_1 \mathcal{L}_{\phi_{\Delta\theta}} + \alpha_2 \mathcal{L}_{\phi_{\text{vel}}}$$

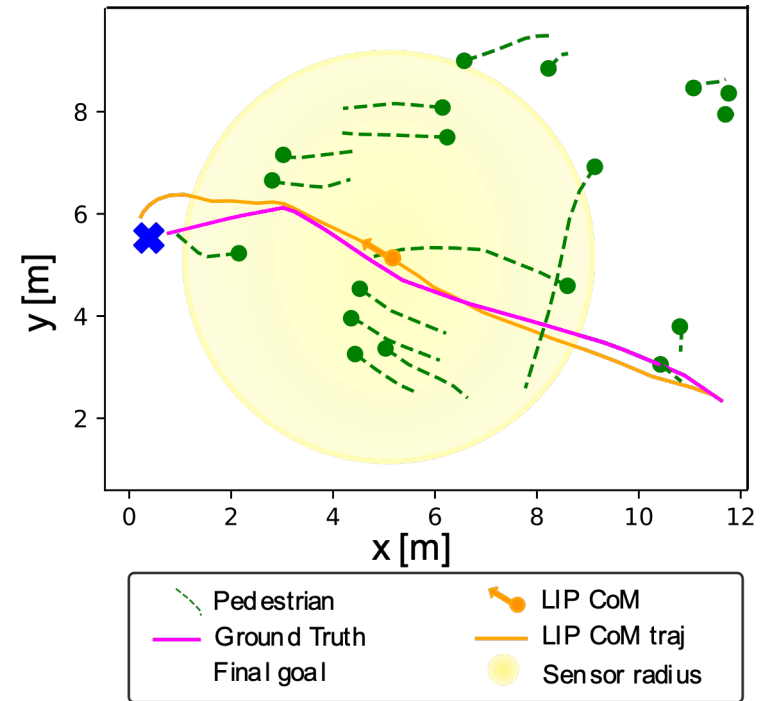
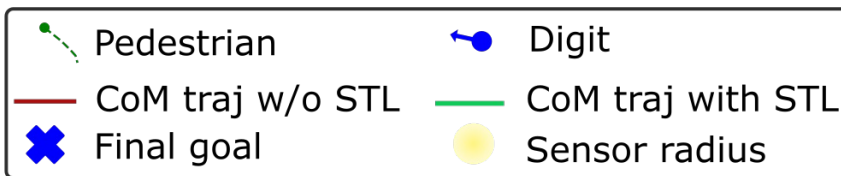
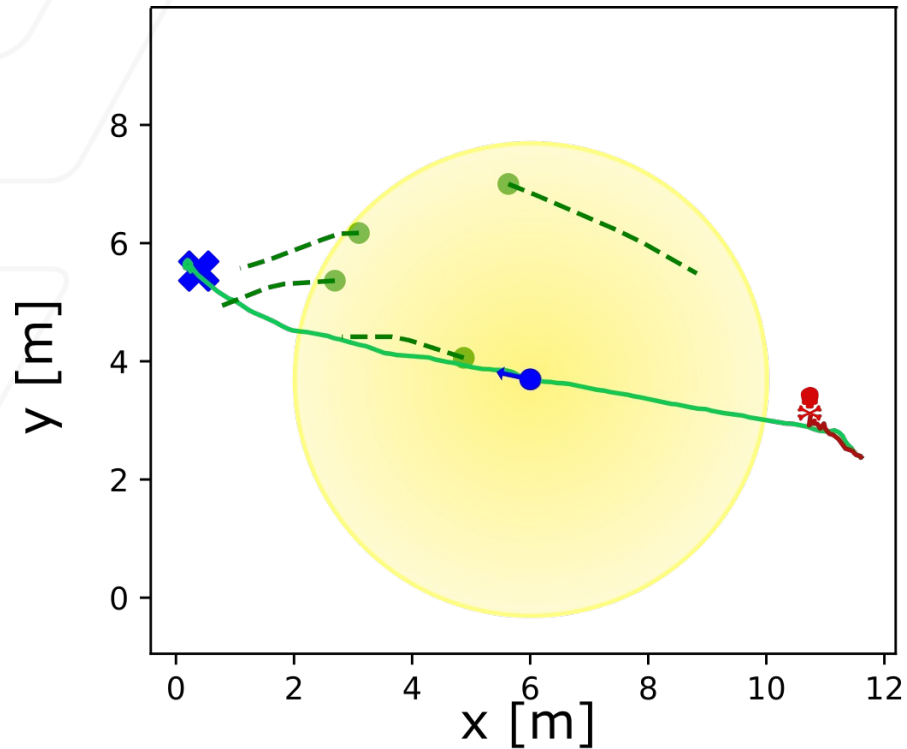
Social Path Planner with STL results



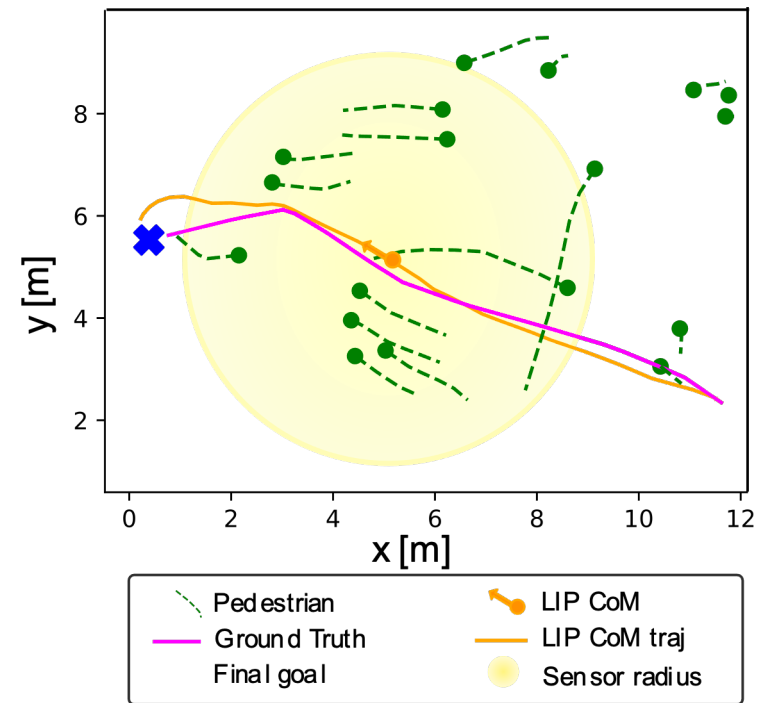
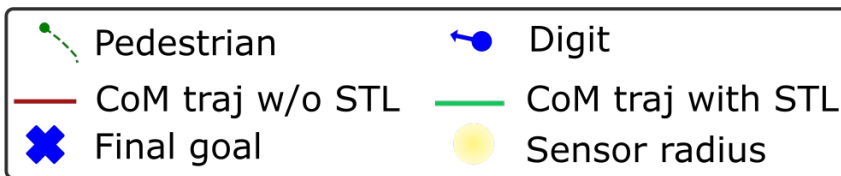
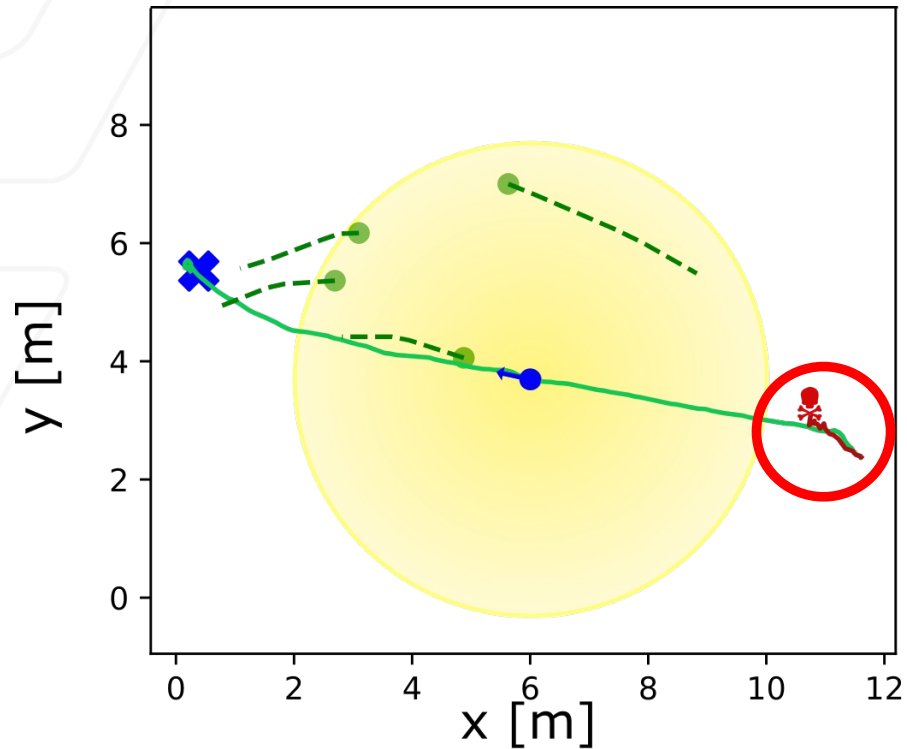
Bipedal Social Path Planner Results



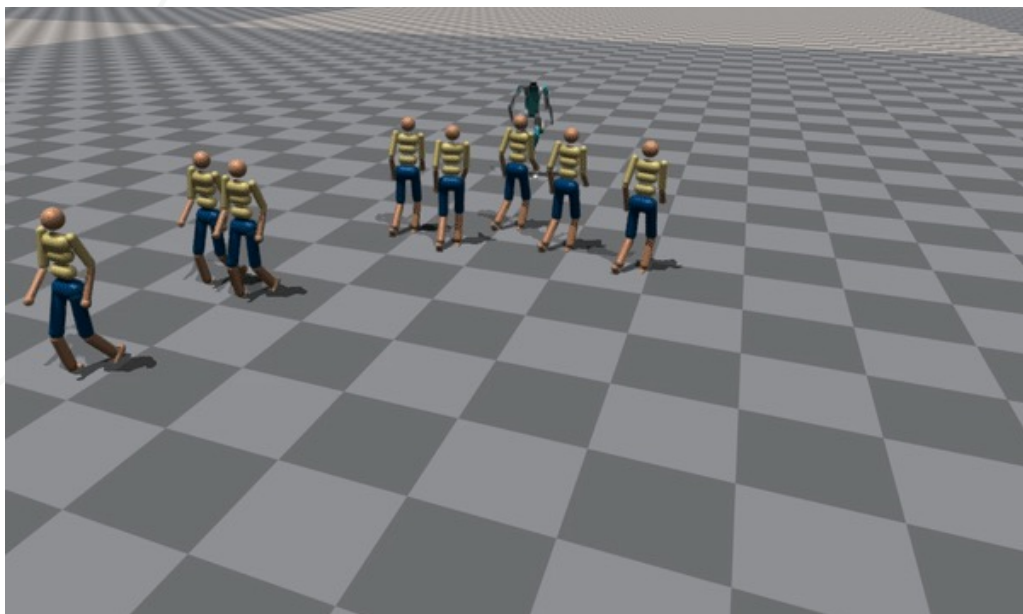
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Bipedal Social Path Planner Results



Preliminary Results



Ongoing work

- Predicting **social reachable corridors** parameterized as zonotopes

$$\mathcal{Z}(c, G) = \{c + G\beta \mid \|\beta\|_\infty \leq 1\}$$

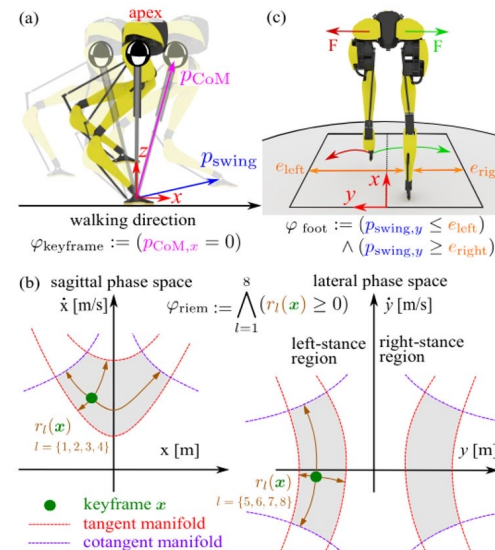
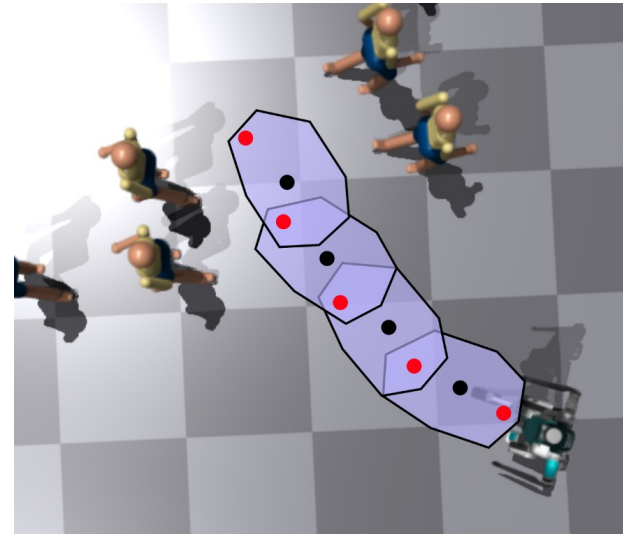
$$\hat{\mathcal{Z}}_{[t, t_{f-1}]}^{\text{ego}} = [c_t, G_t, \dots, c_{t_{f-1}}, G_{t_{f-1}}]$$

$$\mathcal{L}_{\mathcal{Z}} = f(\mathcal{T}^{\text{ego}}, \hat{\mathcal{Z}}^{\text{ego}}) + \|G\|$$

- Evolved STL specification for **locomotion stability** [5]

$$\phi_{\text{loco}} = \diamond_{[T^k, T^{k+1}]}(\phi_{\text{keyframe}} \wedge \phi_{\text{riem}}) \wedge (\square \phi_{\text{foot}})$$

[4] Gu, Zhaoyuan, et al. submitted 2023



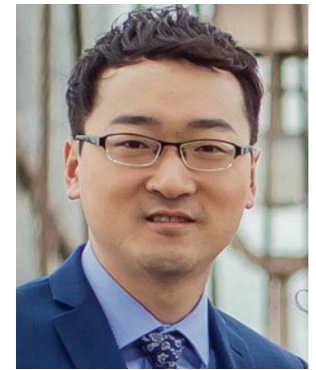
Authors

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